

Statistical Learning of Knowledge from Sequential Data

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ARTIFICIAL
INTELLIGENCE
RESEARCH GROUP

OUTLINE

- ▶ Introduction
- ▶ Modelling Method
- ▶ Application 1: Agent Behaviour
- ▶ Application 2: Music Cognition
- ▶ Future Work and Open challenges

- ▶ **Introduction**
- ▶ Modelling Method
- ▶ Application 1: Agent Behaviour
- ▶ Application 2: Music Cognition
- ▶ Future Work and Open Challenges

Who We Are

- ▶ Prof. Geraint Wiggins
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Research Interests

- ▶ Computational Creativity:

*leaves behind the problem solving paradigm, and moves forward to **problem-seeking** approaches.*

- ▶ Predictive Statistical Systems
- ▶ Learning and Reasoning Systems
- ▶ Cognitive Architectures: *The Information Dynamics of Thinking* (IDyOT: Wiggins, 2020)

INTRODUCTION

MY RESEARCH INTERESTS

Representation and **learning** of hierarchical, cognitive knowledge structures.

Knowledge Representation

- ▶ Hierarchical knowledge structures.
- ▶ Formal ontology, logic and reasoning.
- ▶ Programming languages and type theory.

Knowledge Learning

- ▶ Statistical models of perception and cognition.
- ▶ Information theory
- ▶ Unsupervised learning of knowledge structures from sequence data.

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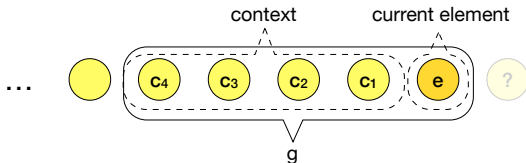
Objective Unsupervised learning of knowledge from statistical patterns in sequence data.

- ▶ Our method is based on *The Information Dynamics of Music* (IDyOM: Pearce, 2005).
- ▶ IDyOM uses variable-order markov models.
- ▶ IDyOM is one of the progenitors of IDyOT.

METHOD

N-GRAMS MODELS AND MAXIMUM LIKELIHOOD

N-gram models are the simplest way to model to a sequence of symbols.



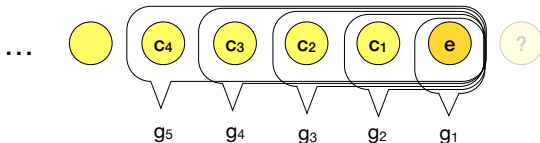
Maximum Likelihood:

$$ML(e, c) = \frac{\text{count}(e, c)}{\sum_{x \in T} \text{count}(x, c)}$$

METHOD

THE PREDICTION BY PARTIAL MATCH (PPM) ALGORITHM

Prediction by partial match (PPM: Cleary & Witten, 1984) combines n-gram predictions of different orders.



PPM:

$$p(e, c) = \alpha(e, c) + \gamma_4 \cdot \alpha(e, c') + \gamma_3 \cdot \alpha(e, c'') + \gamma_2 \cdot \alpha(e, c''') + \gamma_1 \cdot \alpha(e, []) + \gamma_0$$

METHOD

EVALUATING PREDICTIVE MODELS USING INFORMATION

Information (Shannon, 1948) can be used to evaluate the predictive models.

- ▶ Information content quantifies unexpectedness.
- ▶ Entropy quantifies uncertainty.
- ▶ Mean information content quantifies model fit.

Information Content:

$$IC(e, c) = -\log(p(e, c))$$

Entropy:

$$H(c) = \sum_{x \in T} p(x, c) \cdot IC(x, c)$$

METHOD

DEALING WITH MULTIDIMENSIONAL SEQUENCES

Multi-dimensional sequences are modelled using Multiple Viewpoint Systems (Conklin & Witten, 1995).



Element	e1	e2	e3	e4	e5	e6
Pitch	G	G	D	B	A	G
Onset	0	4	8	10	12	16
Duration	4	4	2	2	4	4

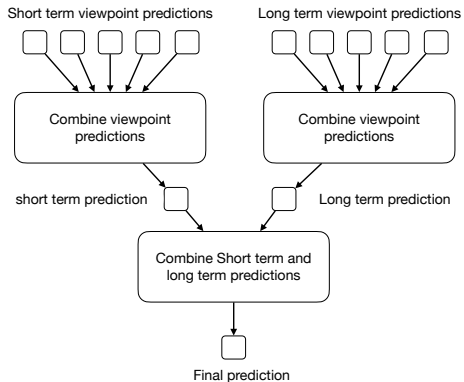
- ▶ IDyOM is a Multiple Viewpoint System.
- ▶ A viewpoint captures a feature of a sequence.
- ▶ Viewpoints can be basic, linked or derived.

METHOD

MODELLING ARCHITECTURE

Viewpoint predictions are combined to create long-term and short-term models.

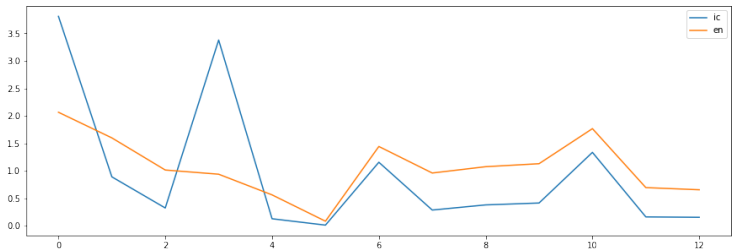
- ▶ A short-term model is trained incrementally on a sequence.
- ▶ A long-term model is pre-trained with example sequences.



METHOD

SEGMENTATION OF SEQUENCES

Information content and entropy profiles are used to locate the boundaries between statistically salient sub-sequences.



- Expectation plays a role in boundary perception and grouping (Pearce et al., 2010)

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APPLICATION 1: AGENT BEHAVIOUR

OVERVIEW

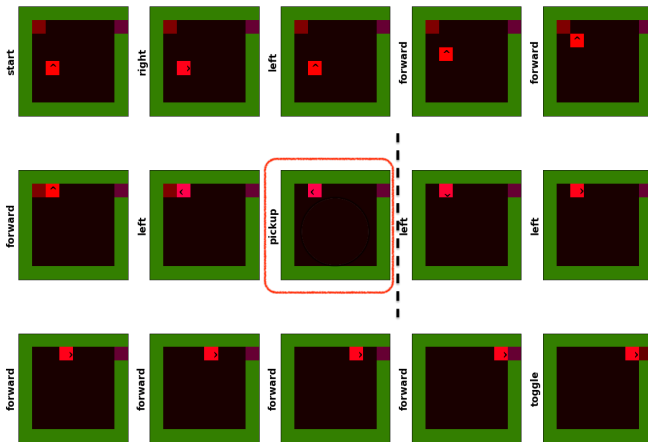
Objective Unsupervised learning of sub-task knowledge from agent behaviour sequence data.

- ▶ Partial observability, dynamic environments, hidden rewards and explainability are problems for RL models.
- ▶ Incorporating knowledge about sub-tasks can mitigate these problems.

APPLICATION 1: AGENT BEHAVIOUR

A SIMPLE TASK WITH TWO SUB-TASKS

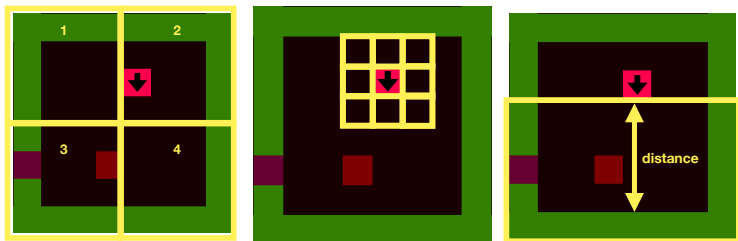
A Gridworld agent must open a door by first picking up a key and then unlocking the door.



APPLICATION 1: AGENT BEHAVIOUR

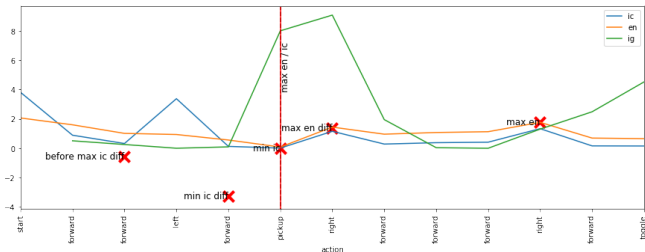
VIEWPOINT REPRESENTATION OF GRIDWORLD

Basic viewpoints capture the current state of the grid (from a birds-eye and a first-person perspective) as well as the last action performed.



APPLICATION 1: AGENT BEHAVIOUR

SUBTASK DETECTION



97% of boundaries correctly identified using minimum information content.

- ▶ First-person viewpoints perform best.
- ▶ Bi-gram models perform best.
- ▶ The short-term models don't help.
- ▶ Model selection by mean IC not optimum for segmentation.

APPLICATION 1: AGENT BEHAVIOUR

NEXT STEPS

- ▶ Study more complex tasks.
- ▶ Define a more general viewpoint representation.
- ▶ Perform automatic segmentation.
- ▶ Perform classification of segments.

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APPLICATION 2: MUSIC

OVERVIEW

Objective Unsupervised learning of perceptual and cognitive representations of musicological structure from sequence data.

- ▶ Music is important and challenging from the perspective of computational creativity.
- ▶ Predictive models of music sequences might provide statistical insight into general perception and cognition.

A CORPUS OF 1000 FOLK MELODIES



APPLICATION 2: MUSIC

VIEWPOINT REPRESENTATION OF MUSICAL MELODIES

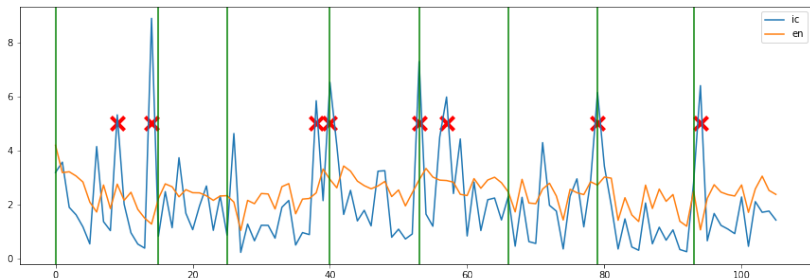
Viewpoints are used to construct an extremely rich representation of musical sequences.

- ▶ Basic viewpoints capture note attributes.
- ▶ More complex viewpoints capture musical relationships between notes.

APPLICATION 2: MUSIC

PHRASE BOUNDARY DETECTION

Musical phrase boundaries correspond closely with prominent features in the information profiles of melodies.



APPLICATION 2: MUSIC

NEXT STEPS

- ▶ Fine-grained segmentation of musical sequences.
- ▶ Automatic classification of segments.
- ▶ Higher-level predictive models of segment classes.

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Future Work

- ▶ Develop composable and reusable tools.
- ▶ Integrate knowledge representation, learning and reasoning.
- ▶ Higher-level prediction.

Open Challenges

- ▶ What is the best way to generalise viewpoint representations?
- ▶ When can two segments be considered equal?

REFERENCES

- ▶ Wiggins, G. A. (2020). Creativity, information, and consciousness: The information dynamics of thinking. *Physics of Life Reviews*, 34–35, 1–39.
- ▶ Pearce, M. T. (2005). The construction and evaluation of statistical models of melodic structure in music perception and composition.
- ▶ Cleary, J. & Witten, I. (1984). Data Compression Using Adaptive Coding and Partial String Matching. In *IEEE Transactions on Communications*, vol. 32, no. 4, pp. 396-402, April.
- ▶ Shannon, C. E. (1948). A mathematical theory of communication. *Bell System Technical Journal*, 27(3), 379–423 and 623–656.
- ▶ Conklin, D., & Witten, I. H. (1995). Multiple viewpoint systems for music prediction. *Journal of New Music Research*, 24(1), 51–73.
- ▶ Pearce, M. T., Müllensiefen, D., & Wiggins, G. A. (2010). The role of expectation and probabilistic learning in auditory boundary perception: A model comparison. *Perception*, 39(10), 1367–1391.

THANK YOU!



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